

In development, incomplete..



Time Series Analyzer

Used math formulas

Version 1.1.0

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Sorry for my English :-)

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Base statistics

Variance

Name	Variance. (Sample variance).
Used formula	$s^2 = \frac{\sum_{t=1}^N (y_t - \bar{y})^2}{N}$
Parameters	N = count of values
Conditions	If Yt is null, observation is omitted.
History	Added 2010.
Sources	<p><i>MONTGOMERY, D. Introduction to Time Series Analysis and Forecasting. Published by John Wiley & Sons. 2008. ISBN 978-0-471-65397-4.</i></p> <p>Page 28.</p>

Measure of accuracy

Mean absolute error (MAE, MAD)

Name	MAE (Mean absolute error). Can be named as mean absolute deviation (MAD) too.
Used formula	$MAE = \frac{1}{n} \sum_{t=1}^n e_t $
Parameters	e_t = forecast error (residuals)
Conditions	
History	Added 2011.
Sources	<i>MONTGOMERY, D. Introduction to Time Series Analysis and Forecasting. Published by John Wiley & Sons. 2008. ISBN 978-0-471-65397-4.</i> <i>Page 49.</i>

Mean absolute percentage error (MAPE)

Name	MAPE (Mean absolute percent error).
Used formula	$MAPE = \frac{1}{n} \sum_{t=1}^n \left \left(\frac{y_t - \hat{y}_t}{y_t} \right) * 100 \right $
Parameters	Result in percent.
Conditions	
History	Added 2010.
Sources	<p><i>MONTGOMERY, D. Introduction to Time Series Analysis and Forecasting. Published by John Wiley & Sons. 2008. ISBN 978-0-471-65397-4.</i></p> <p><i>Page 180.</i></p>

Mean error (ME)

Name	ME (Mean error). Can be named as average error too.
Used formula	$ME = \frac{1}{n} \sum_{t=1}^n e_t$
Parameters	e_t = forecast error (residuals)
Conditions	
History	Added 2011.
Sources	<i>MONTGOMERY, D. Introduction to Time Series Analysis and Forecasting. Published by John Wiley & Sons. 2008. ISBN 978-0-471-65397-4.</i> <i>Page 49.</i>

Mean percent error (MPE)

Name	MPE (Mean percent error).
Used formula	$MPE = \frac{1}{n} \sum_{t=1}^n \left(\left(\frac{y_t - \hat{y}_t}{y_t} \right) * 100 \right)$
Parameters	Result in percent.
Conditions	
History	Added 2010.
Sources	<p><i>MONTGOMERY, D. Introduction to Time Series Analysis and Forecasting. Published by John Wiley & Sons. 2008. ISBN 978-0-471-65397-4.</i></p> <p>Page 51.</p>

Mean squared error (MSE)

Name	MSE (Mean squared error).
Used formula	$MSE = \frac{1}{n} \sum_{t=1}^n (e_t)^2$
Parameters	e_t = forecast error (residuals)
Conditions	
History	Added 2011.
Sources	<i>MONTGOMERY, D. Introduction to Time Series Analysis and Forecasting. Published by John Wiley & Sons. 2008. ISBN 978-0-471-65397-4.</i> <i>Page 50.</i>

Sum of squares error (SSE)

Name	SSE (Sum of squares error).
Used formula	$SSE = \frac{1}{n} \sum_{t=1}^n e_t^2$
Parameters	e_t = forecast error (residuals)
Conditions	
History	Added 2011.
Sources	http://www.wikihow.com/Calculate-the-Sum-of-Squares-for-Error-%28SSE%29

Information criteria

Akaike`s information criteria (AIC)

Name	AIC (Akaike`s information criteria)
Used formula	$AIC = n * \ln \left(\frac{SSE}{n} \right) + 2k$
Parameters	SSE = sum of squares, k = number of parameters in the model.
Conditions	
History	Added 2011.
Sources	http://coopunit.forestry.uga.edu/Coop_Wkshop/inference_effects/aic_reg.pdf

Akaike`s information criteria - corrected (AICc)

Name	AIC (Akaike`s information criteria - corrected)
Used formula	$AIC_c = n * \ln \left(\frac{SSE}{n} \right) + 2k + \frac{2k * (k + 1)}{n - k - 1}$
Parameters	SSE = sum of squares, k = number of parameters in the model.
Conditions	
History	Added 2011.
Sources	http://coopunit.forestry.uga.edu/Coop_Wkshop/inference_effects/aic_reg.pdf

Bayesian information criteria (BIS)

Name	BIS (Bayesian information criteria)
Used formula	$BIC = n * \ln\left(\frac{SSE}{n}\right) + k * \ln(n)$
Parameters	SSE = sum of squares, k = number of parameters in the model.
Conditions	
History	Added 2011.
Sources	http://www.google.cz/url?sa=t&rct=j&q=Bayesian%2Binformation%2Bcrit erion&source=web&cd=2&ved=0CDIQFjAB&url=http%3A%2F%2Fwww.c hichen6.tcu.edu.tw%2Fteaching%2F%25E8%25AC%259D%25E7%25B 4%25B9%25E9%2599%25BD%25E7%25AD%2589_2nd_BIC- AIC.ppt&ei=Ke-8ToLxNoKCtgfLpvivBg&usg=AFQjCNGHaIUvrAL1XIUXEHptClilmT7EnA &sig2=GaZSSj1k9DvcXS4ezOeqCg

Smoothing

Simple exponential smoothing (first-order)

Name	Simple exponential smoothing
Used formula	$\widehat{y}_T = \alpha y_T + (1 - \alpha) \widehat{y}_{T-1}$
Parameters	alpha = discount factor
Conditions	<p>First value is (by global/section setting):</p> <ul style="list-style-type: none"> a) NULL b) copy of original first value c) average of values
History	Added 2010.
Sources	<p><i>MONTGOMERY, D. Introduction to Time Series Analysis and Forecasting. Published by John Wiley & Sons. 2008. ISBN 978-0-471-65397-4.</i></p> <p><i>Page 177.</i></p>

Simple exponential smoothing (Brown)

Name	Simple exponential smoothing (Brown`s)
Used formula	$\hat{y}_T = \alpha y_{T-1} + (1 - \alpha) \hat{y}_{T-1}$
Parameters	alpha = discount factor
Conditions	First value is (by global/section setting): a) copy of original first value b) average of values
History	Added 2011.
Sources	http://fsi.uniza.sk/kkm/old/publikacie/pp/pp_kap_8.pdf , page 151-152 http://en.wikipedia.org/wiki/Exponential_smoothing

Double exponential smoothing (Holt`s)

Name	Double exponential smoothing (Holt`s)
Used formula	$L_t = \alpha y_t + (1 - \alpha)(L_{t-1} + T_{t-1})$ $T_t = \beta(L_t - L_{t-1}) + (1 - \beta)T_{t-1}$ $\hat{y}_{t+p} = L_t + pT_t$
Parameters	alpha, beta = discount factors
Conditions	First value: Copy of first original Y value, trend part = 0
History	Added 2011.
Sources	http://www-rocq.inria.fr/axis/modulad//Workshop_Franco_Bresilien/programme/MaiaDeCarvalho_WFB2009.pdf http://fsi.uniza.sk/kkm/old/publikacie/pp/pp_kap_8.pdf

Triple Holt-Winters Exponential Smoothing

Name	Holt-Winters triple exponential smoothing
Used formula	$L_t = \alpha \left(\frac{y_t}{S_{t-s}} \right) + (1 - \alpha) * (L_{t-1} + T_{t-1})$ $T_t = \beta (L_t - L_{t-1}) + (1 - \beta) * T_{t-1}$ $S_t = \gamma \left(\frac{y_t}{L_t} \right) + (1 - \gamma) * S_{t-s}$
Parameters	alpha, beta, gama = discount factors
Conditions	<p><u>Only if seasonal support is active in project.</u></p> <p>First value:</p> <p>L = Copy of first original Y value T = 0 S = 1</p> <p>s = seasonal length</p>
History	Added 2011.
Sources	<p>http://fsi.uniza.sk/kkm/old/publikacie/pp/pp_kap_10.pdf</p> <p>http://www.it.iitb.ac.in/~praj/acads/seminar/04329008_ExponentialSmoothing.pdf</p> <p>http://artax.karlin.mff.cuni.cz/~venco2am/vyuka/pms3/Holt-Winters.pdf</p>

Regressions

Gompertz curve

Name	Gompertz curve
Used formula	$Y = k \times \alpha^{\beta^x}$
Information	Computed by the partial sum method.
Conditions	Original data $Y > 0$ (no negative values).
History	Added 2010.
Sources	http://mathworld.wolfram.com/GompertzCurve.html

Modified exponential regression

Name	Modified exponential regression
Used formula	$Y = \gamma + A \times B^x$
Parameters	
Conditions	
History	Added 7 / 2011.
Sources	<i>SMITH, K. TIME SERIES ANALYSIS, U.S. Agency for international Development Manila, Philippines, 1975. Page 29.</i> http://pdf.usaid.gov/pdf_docs/PNABI046.pdf

Polynomial regression

Name	Polynomial regression
Used formula	$y = a_0 + a_1x + a_2x^2 + a_3x^3 + \dots + a_mx^m$
Parameters	Maximum model degree is possible change in regression section settings.
Conditions	
History	Added 2010.
Sources	http://en.wikipedia.org/wiki/Polynomial_regression

Transformations

Ln (y)

Name	Transformation - Ln(y)
Used formula	$f(y) = \ln y$
Conditions	$y > 0$
History	Added 5/2011.
Sources	<p>SAS:</p> <p><i>Link:</i> http://support.sas.com/documentation/cdl/en/etsug/60372/HTML/default/viewer.htm#etsug_similarity_sect015.htm</p> <p>HANZAK, TOMAS: <i>Decomposition methods for time series with irregular observations</i>, page 65.</p> <p><i>Link:</i> www.quantitative.cz/.../decomposition-methods-for-time-series-with-irregular-observations-tomas-hanzak-2007-in-czech.pdf</p>

Square root (y)

Name	Transformation - Square root (y)
Used formula	$f(y) = \sqrt{y}$
Conditions	$y \geq 0$
History	Added 5/2011.
Sources	SAS: <i>Link:</i> http://support.sas.com/documentation/cdl/en/etsug/60372/HTML/default/viewer.htm#etsug_similarity_sect015.htm

Standardization (y)

Name	Transformation - Standardization(y)
Used formula	$f(y) = \frac{y - \mu}{\sigma}$
Parameters	μ - average (y) σ - standard deviation(y)
Conditions	Standard deviation $\neq 0$.
History	Added 5/2011.
Sources	SAITTA, SANDRO: Link: http://www.dataminingblog.com/standardization-vs-normalization/

Normalization (y)

Name	Transformation - Normalization(y)
Used formula	$f(y) = \frac{y - y_{min}}{y_{max} - y_{min}}$
Parameters	
Conditions	Denominator $\neq 0$, if is, then $f(y) = \text{null}$.
History	Added 5/2011.
Sources	SAITTA, SANDRO: Link: http://www.dataminingblog.com/standardization-vs-normalization/

Hypothesis testing

Kolmogorov-Smirnov

Name	Kolmogorov-Smirnov
Used formula	<p>Test value based on:</p> $D_i = \left \text{rel} F_i - \text{rel} \hat{F}_i \right $ $D'_i = \left \text{rel} F_{i-1} - \text{rel} \hat{F}_i \right $
Parameters	<p>Critical values:</p> <p>http://www.kmt.zcu.cz/person/Kohout/info_soubory/letnisem/ruzne/KSjednovyber.pdf</p>
Conditions	
History	Added 8/2011.
Sources	<p>MARR, PAUL: http://webpace.ship.edu/pgmarr/Geo441/Examples/Normality%20Tests.pdf</p> <p>http://webpace.ship.edu/pgmarr/Geo441/Lectures/Lec%204%20-%20Normality%20Testing.pdf</p>

Kolmogorov-Smirnov (Lilliefors variant)

Name	Kolmogorov-Smirnov (Lilliefors variant)
Used formula	<p>Test value based on:</p> $D_i = \left \text{rel} F_i - \text{rel} \hat{F}_i \right $ $D'_i = \left \text{rel} F_{i-1} - \text{rel} \hat{F}_i \right $
Parameters	<p>Critical values:</p> <p>http://www.utdallas.edu/~herve/Abdi-Lillie2007-pretty.pdf</p>
Conditions	
History	Added 8/2011.
Sources	<p>MARR, PAUL: http://webpace.ship.edu/pgmarr/Geo441/Examples/Normality%20Tests.pdf</p> <p>http://webpace.ship.edu/pgmarr/Geo441/Lectures/Lec%204%20-%20Normality%20Testing.pdf</p>

W/S

Name	W/S
Used formula	<p>Test value based on:</p> $q = \frac{w}{s}$
Parameters	<p>w - data range (max-min) s - standard deviation (-1)</p> <p>Critical values: http://www.watpon.com/table/normality.pdf</p>
Conditions	
History	Added 8/2011.
Sources	<p>MARR, PAUL: http://webspace.ship.edu/pgmarr/Geo441/Examples/Normality%20Tests.pdf</p> <p>http://webspace.ship.edu/pgmarr/Geo441/Lectures/Lec%204%20-%20Normality%20Testing.pdf</p>

D`Agostino

Name	D`Agostino
Used formula	<p>Test value (D) based on:</p> $T = \sum \left(i - \frac{n+1}{2} \right) X_i$ $D = \frac{T}{\sqrt{n^3 SS}}$ <p>where:</p> <p>SS - sum of squares of the data, n - sample size, i - order of observation.</p>
Parameters	<p>Critical values:</p> <p>http://webpace.ship.edu/pgmarr/Geo441/Tables/D%27Agostino%20D%20Test.pdf</p>
Conditions	
History	Added 9/2011.
Sources	<p>MARR, PAUL:</p> <p>http://webpace.ship.edu/pgmarr/Geo441/Lectures/Lec%204%20-%20Normality%20Testing.pdf</p>

Shapiro-Wilk

Name	Shapiro-Wilk
Used formula	<p>Test value (SW) based on:</p> $SW = \frac{\left(\sum_{i=1}^m a_i(n) (X_{(n-i+1)} - X_{(i)}) \right)^2}{\sum_{i=1}^n (X_i - \bar{x})^2}$ <p>where: ai - is coefficients.</p>
Parameters	<p>Critical values, coefficients: http://sci2s.ugr.es/keel/pdf/algorithm/articulo/shapiro1965.pdf</p>
Conditions	
History	Added 9/2011.
Sources	<p>http://sci2s.ugr.es/keel/pdf/algorithm/articulo/shapiro1965.pdf http://dspace.upce.cz/bitstream/10195/32424/1/CL299.pdf</p>

Jarque-Bera

Name	Shapiro-Wilk
Used formula	<p>Test value (JB) based on:</p> $JB = \frac{n}{6} \left((Skew\ x_s)^2 + \frac{(Kurt\ x_s)^2}{4} \right)$
Parameters	<p>Critical values:</p> <p>Normal: <i>chi-square</i>, <i>df=2</i>: http://www.psychstat.missouristate.edu/introbook/chisq.htm</p> <p>Lagrange multiplier (LM), Advanced Lagrange multiplier (ALM): http://mpr.ub.uni-muenchen.de/19155/1/MPRA_paper_19155.pdf</p>
Conditions	
History	Added 9/2011.
Sources	http://www.alglib.net/hypothesistesting/jarqueberatest.php